

Appendix A

The transformation matrix T

We give the matrix T which transforms the generator z in its Jordan form $J = TzT^{-1}$. Since $T \in GL_{154}(3)$, we display T only as a MAGMA input.

Appendix B

The 44-dimensional matrices

We present the reduced matrices on $V_{154}(z^2, 1)$. These are the upper left 44×44 -submatrices of TMT^{-1} , $M \in \{X, Y, \rho\}$.

Appendix C

The 44-dimensional matrices obtained by the Meataxe

We present the 44-dimensional matrices X_M , Y_M , ρ_M and a_M obtained by using the Meataxe program in MAGMA [2]. We give also a matrix t_{44} , obtained using the MAGMA function `IsIsomorphic` for modules such that $t_{44}M_M t_{44}^{-1} = M_{44}$ where $M_M \in \{X_M, Y_M, \rho_M\}$ and M_{44} is the corresponding matrix in $\{X_{44}, Y_{44}, \rho_{44}\}$.

$$X_M = \left(\begin{array}{c} 00101122200211202002000201110122121222002121 \\ 12212000010011002021012122100010202200111122 \\ 1221001100101002020220120000211220120000022 \\ 00101101122221101212001120000122000002021101 \\ 2101110111220010112222211210221022111221102 \\ 11202102011202021122212102210211002001121100 \\ 10210121002112101212210212220221021021202112 \\ 0002212111011111201211200010102101201110102 \\ 1111000222222211111002110102020100111101110 \\ 12200110221102222200012001210102020221200011 \\ 122102101000021021011122110122200020000101 \\ 021211121201220101212112002010220200222220 \\ 00000101102202020222021100122001202000212 \\ 0020012111201102012100221002020100121101210 \\ 01212012102202011220111002220000101211120111 \\ 0000112002110122222022122000221210212120202 \\ 2102211000122211020020201100022111110012020 \\ 22102012012100011010210001020010101021111012 \\ 002100110010210211001102020201112021010122 \\ 12112220012122122011210020220122120210210220 \\ 2201011020111201101221201022002000122222220 \\ 02102022102102002210000112020000200210201120 \\ 01210012002110202222011010000010021112021021 \\ 20120101222022000202202001220010002211211100 \\ 00012120011120110001100022100211012022001100 \\ 22201102010212121012011122210211212220120121 \\ 01112110001220200120020220020201200021210020 \\ 10222020200000002000101102210022121221202220 \\ 12100012022102101222210110102201101200120202 \\ 02000122200210002012122101210002100101001222 \\ 11101222021022222001101101210000202220022221 \\ 21212100021012022012002000200101022010221 \\ 01011202121020011120011200000020021200121121 \\ 22022210122020200001010202010221202000100100 \\ 2100111012100022111121210010021102211211101 \\ 120011121022220120020101110010201001201201201 \\ 02000121002202201102011212200221222022002212 \\ 210022210002020221022121210010201021111001 \\ 01020102110020202201112020200221101111001120 \\ 112210111211211100102000120122111000021210 \\ 01001121202120220200002222020221012010212220 \\ 1012222011011000111212022210201110121002102 \\ 10101111202211102010101122200020220001001010 \\ 10011012012111000212201112010010121212121001 \end{array} \right)$$

$$Y_M = \left(\begin{array}{c} 02010201011100110102001120022211021120011002 \\ 10202012021102000020110022111122102001102000 \\ 00200221202002200112202021010212222112122100 \\ 20012121022011120122012112011102100011110002 \\ 2221021221221010201011022020211211202202210 \\ 20122202121201211201002001011102200120202211 \\ 20220002102012220011120012221120100011210010 \\ 111111200120020022211100220201002010000121 \\ 22212010102212020212000122121220101210011222 \\ 01222111012120020010210211202212022022102122 \\ 10121200200102012220120221021222000011121000 \\ 01021101021020112011220221201210012212121221 \\ 20012222110022100022222000121200001011211112 \\ 21221112211200112101100100202200121120102222 \\ 20211210011112200222010101110202122122121211 \\ 22201222010022112121000120012201021002010112 \\ 11000202110121002200112212022021001111101200 \\ 11120211202000202101211011110101212101122102 \\ 21020221221122110101001021211221111112201 \\ 02010102110012121100120211120021112100212002 \\ 00221101021200012211002021000212101200202011 \\ 0120112222200000010200102100020020201101202 \\ 12122100021220121221200220101002101212010021 \\ 11210222202112012120012200220121110201012220 \\ 1021211121222221120022000220012011100002121 \\ 2211202021001122022011222201011010011112112 \\ 20011121211210200220021011000012011122012220 \\ 121121220012222201020110221220022220100010 \\ 0220221212022201222020201202110111001200201 \\ 00102012101110010221022221021202120001000110 \\ 1022122210210120112000202020002110010112100 \\ 22121121120100022000202210122120112020221222 \\ 11000012102111022200211102020210221221121001 \\ 10020111011112201021120222020212111112101020 \\ 110121021112021200101010002120020112100222 \\ 01020212121210201001110122010220210002212222 \\ 12011012220122200110212210201222000110121110 \\ 00112220011020121112012202122101000101201010 \\ 12100202000012221010011221112120010112022200 \\ 22011221101122100210121202012202201100200221 \\ 02101112101202012121120112211010200100211111 \\ 10022001210110212212101112210211220102021111 \\ 01122110021210000101222220211122012122000022 \\ 00121122110000120001000222101112200111022110 \end{array} \right)$$

$$\rho_M = \left(\begin{array}{c} 1102102001100221100221012201210221120012011 \\ 0010012220020112100102022120211010200002121 \\ 01221110110010110212211010212122121100201220 \\ 01101202221112000102121120112021012101122000 \\ 21210210000120012002110200120101200010221112 \\ 01200001011201202011212200210121022122012200 \\ 11202101122120012211220101101212212022120221 \\ 20120021220120121101101210212120020010211002 \\ 02110012112102221012002212021212012212000220 \\ 22222110020200002201110010022210221122001122 \\ 0112202210010122220211110211210201110221100 \\ 20201120102000021100001010021101112110220001 \\ 12100100021212000221011121200020220220112211 \\ 20220221001102200220012011021112210212101020 \\ 21122112111222022200120020210022022102202200 \\ 111121210111021222002002010101110110110210 \\ 00210011201120021202022121210010010012210012 \\ 1010002200100021111220110012221122210212202 \\ 00221010021011101101102001111202121021210101 \\ 00011022222122002201110202202101120011212112 \\ 00011120120100010201012012210200011211120001 \\ 1221111211202010112210211002200112011021102 \\ 21011022220200221112010100100100121110010012 \\ 22022111020021021001120002220121220101201110 \\ 21222202010210001210120012120112200102221201 \\ 00121211021021210212010112021001100210110010 \\ 22002201111212000220120001110100022010012102 \\ 0210102100201122121010222202210012212200101 \\ 020012120221110212022101220222101110100222 \\ 010221022211021112102011010220112221012101 \\ 1011110212221001001220120111021110222212210 \\ 12102111121002101110122111000100020210202001 \\ 00022222021110010112201022102012111011021020 \\ 02011000101022012200212101002100020111112111 \\ 20002202220102200020011012000112221221200021 \\ 0022021220001111200221010112122000210012102 \\ 22121120211111010222120010221011002001202100 \\ 2110111111002211100212102020120211010221010 \\ 0001021200210000122211210010121210000112002 \\ 02110111222210021110020120221202010110100120 \\ 102121022211222220120121211212120010010011 \\ 02111021021011100000210012112200011220112221 \\ 11120202002200011211120221001121002002211100 \\ 01100112022122102222211100102220222021101100 \end{array} \right)$$

$$a_M = \left(\begin{array}{c} 20022120000001100001102012122000102210011010 \\ 12102001120012002210212020100201022020200212 \\ 0020010101021121120200200112222111100021110 \\ 2101202121111000101202221022222012121122110 \\ 022200100012111010211022211001002020222201 \\ 12222200211202202211211202022000222010210202 \\ 1120120010102110111122022000121121120112021 \\ 0002012112012012020100111212112010010122 \\ 002011121020202122210002110100112101002221 \\ 12022002200022000110120201220202220211200201 \\ 22021002021012110212020120001212100221121201 \\ 112021021012220002210122111212011010211211 \\ 11202022012121210021012022221212011000021220 \\ 1220101001102102002000010020200000011221120 \\ 21110002001112120011022002021202020102201212 \\ 21021022121020121212102200110102200102022021 \\ 101222020200012100002122022202100200120221 \\ 00201010010120002121002201110120012121020002 \\ 21000222000121000001220112002201012021122101 \\ 1012211002221120212011211221112211022101020 \\ 01220120122000102101120112002110020022211001 \\ 20110112011102101120120122010021212000012121 \\ 12222202211120112012102210112001021211022222 \\ 11020122011002122212012001110120011120110211 \\ 221112012012000201101101201010020000011220 \\ 10101210201220220001101202020022110010210120 \\ 0122100021212001222121012021202221102110210 \\ 12101121111211001001010101101021012012200 \\ 0200211202202110110021201210211001010212110 \\ 2220111201202010012202121011202001210022220 \\ 0211021021221210221000011222002220022101100 \\ 0120221221220122211212101021112010010121120 \\ 10122012201112102000112020102111200002121000 \\ 0120110201211000221200222000211222020021022 \\ 0210210010120201120020222221010110011020210 \\ 210011211201120101210200021011101021011101 \\ 22221020102200221102102222111121222210001122 \\ 01001021101110012001000020122102212121100102 \\ 021121001120011111022210210112201012002021 \\ 10220211002022010202210011000120100022100002 \\ 21200122110011110001122020011001122101122200 \\ 2020200210210111122002122212122112102010212 \\ 11120212022102211000211020022200212101211020 \\ 00202001021220021100122121200100101012210000 \end{array} \right)$$

$$t_{44} = \left(\begin{array}{c} 10201211220211222110221011021122020210212020 \\ 0012222021210110011011210220221022002211211 \\ 10012202110100202111121020202020010210202020 \\ 11010002211020101001001010021221121210202102 \\ 21220102021220010001210110012222010200222211 \\ 1120222011211012010211001120220211022010021 \\ 1120120102202200020222022001001012002110201 \\ 12021220102220200000220220112002222011112100 \\ 2100022121122202220221222212012122120211020 \\ 0011102212020112011122212002012112002202010 \\ 12022001010101212002021011110212020012212220 \\ 00021000000111222001222011112010112022010121 \\ 0200122001021201010121112020202211002120222 \\ 1221020210122220112120102200002102002210020 \\ 00022011011220210220200101011112010122121010 \\ 00212200111122002102010220002001001211211000 \\ 2202001012120112110100112021111121011112211 \\ 2110111102210100120110210020200101110012021 \\ 010001121121202121022222112010120020000112212 \\ 10100212110120222222110202221210001001111010 \\ 20101211000210012010102100110010020210111211 \\ 0111102212122010202021001211022201002101000 \\ 0002212201000011001100101001002002211211011 \\ 000112102112120120121001111011110222022102 \\ 21202222020002010002002122212011011102110021 \\ 12110101211102111120021011121011100122122012 \\ 02021221010210122012112211021101200111122222 \\ 02210210012100011002002012000021110122201100 \\ 02020100021201202200201112211110112110211010 \\ 21210002022202011220002102120211122202021100 \\ 12110100121021221210102210110001100000112 \\ 12011200112221200122111112220002102011220002 \\ 0021101111120002222200021020122022011010121 \\ 12120120211120210012110001112001221201201100 \\ 20220012012010022000110111201220220102102120 \\ 12011000220200200001212001210020011120010101 \\ 21012110001112220211112100100100102112021000 \\ 01120222021112211002021111222121000021201222 \\ 11011011221022102122220110022010122011211010 \\ 00210021111002000011200011122122010211201000 \\ 0122011021110211102220122210000010011010122 \\ 1101021122022202220212220220010222001000120 \\ 1011202020002212221120100000010211120210011 \\ 10122212001100220112121222210000100121120020 \end{array} \right)$$

Appendix D

The generators of $C_{GL_{44}(3)}(< X_{44}, Y_{44}, \rho_{44} >)$

We present the generators of $C_{GL_{44}(3)}(H)$ with $H := < X_{44}, Y_{44}, \rho_{44} >$. These matrices have been achieved as follows. We use MAGMA [2] to determine the indecomposable summands of $V_{44}|_{< X_{44}, Y_{44}, \rho_{44} >}$. We hold that $V_{44}|_{< X_{44}, Y_{44}, \rho_{44} >} = V_{1,A} \oplus V_{1,B} \oplus V_{12} \oplus V_{15,A} \oplus V_{15,B}$ where $\dim V_{i,K} = i$. Moreover $V_{1,A} \not\simeq V_{1,B}$ and $V_{15,A} \not\simeq V_{15,B}$ and $V_{15,B}$ is a tensor product of $V_{15,A}$ with a 1-dimensional module [21]. Furthermore we have that V_{12} is irreducible but not absolutely irreducible. It is a 6-dimensional module over $GF(9)$ (see e.g. [22]). Therefore the centralizer of $H|_{V_{12}}$ has order at most eight. According to [21], we have that $|C_{GL_{15}(3)}(H|_{V_{15,A}})| = |C_{GL_{15}(3)}(H|_{V_{15,B}})| = 2 \cdot 3$. This proves that $|C_{GL_{44}(3)}(H)| \leq 2^7 \cdot 3^2$.

We now use the MAGMA program `IsIsomorphic` for modules to hold matrices $t_i \neq t_{44}$ ($i = 1, 2, 3, 4, 5$) to conjugate the generators obtained by the meataxe. Then $s_i = t_i t_{44}^{-1}$ centralizes X_{44} , Y_{44} and ρ_{44} . We display these matrices as s_i on the following pages. Using MAGMA, we hold $|< s_1, s_2, s_3, s_4, s_5 >| = 2^7 \cdot 3^2$ thus $< s_1, s_2, s_3, s_4, s_5 > = C_{GL_{44}(3)}(H)$.

Appendix E

The suitable candidates $a_{44,i}$

We present the suitable candidates $a_{44,i}$ obtained by conjugating the $t_{44}a_Mt_{44}^{-1}$ in $C_{GL_{44}(3)}(< X_{44}, Y_{44}, \rho_{44} >$ in the way described in Chapter 4.

$$a_{44,1} = \left(\begin{array}{c} 0211121112100120200122020201100211112020020120 \\ 02011001101211011110220022002212010222110 \\ 21202001121210011100200220101112000121101202 \\ 02221100102220210220022222212202002002111 \\ 120021020212020200011102011100002122022220 \\ 20122011202122021012212101102211001020102222 \\ 0111202221222121111210011101211020102120211 \\ 0021102210020110201111002212010201201100002 \\ 02221010012200020011120120011102221002011220 \\ 02021011102100021211221102101120221012212200 \\ 1220211211102000002111120221212101212200021 \\ 2021202022002010220220122110022201110102000 \\ 0102102212011210112110010221201211000222221 \\ 22210120111021001200012002100021020020121111 \\ 21021122120100200202211110001002210112010210 \\ 10201000121202002002211012022211001021121122 \\ 12211120000222011012210002011010100111221022 \\ 1202012220222202201111010221120210001212101 \\ 2121210110010200021202100012000012201002111 \\ 2212211102002002101000022121021112020020120 \\ 0100012011110100200120122022121121021102020 \\ 21101120101012022102022201021122021210002110 \\ 21111212200100202111210110021020000200010022 \\ 0220202110121222021110000122200022210112101 \\ 1102112021212110010121020222111122021210002110 \\ 00222210012210210102020211110110011121001112 \\ 22110211112020210211102020011111100120000101 \\ 21111221122211211002212012000122221010010210 \\ 001001021200101100122211221021121101202221 \\ 00011202212022010111001122121200020021010002 \\ 02211201112000011020010111201120220112112222 \\ 10100021101220102020220000222011202111021002 \\ 1200220000121221020221220120222010000001010 \\ 11011201111020100220001011112102001011101221 \\ 21122002220221220110002220221011010021221221 \\ 00011101220220111102102210002022020010101202 \\ 2001220011200120112211120120102220101201002 \\ 0001201112001100011101211010201121100012221 \\ 0222001122202101211010122200222202122222222 \\ 0112221011211001110200011120221122112022221 \\ 02200021122010010200201012121001022011000222 \\ 0102220021212101212110222110122122200021202 \\ 0002211122002012021110012221020111212102211 \\ 0111121100200101111202112001212121100222221 \end{array} \right)$$

$$a_{44,2} = \left(\begin{array}{c} 02111211121001202001220201100122221010010210 \\ 0201100110121101111022002220011121020111221 \\ 21202001121210011100200220102221000212202101 \\ 022211001022202102200222221121101001001221 \\ 12002102021202020001110201110000121101111012 \\ 20122011202122021012212101101122002010201111 \\ 01112022212221211112100111011220102012101020 \\ 0021102210020110201111002211020102102200000 \\ 02221010012200020011120120012201112001022111 \\ 02021011102100021211221102102210112021121102 \\ 12202112111020000021111120222121202121100010 \\ 20212020220020102202201221100111102220201000 \\ 0102102212011210112110010221102122000111110 \\ 22210120111021001200012002100012010010212222 \\ 21021122120100200202211110002001120221020121 \\ 10201000121202002002211012021122002012212212 \\ 1221112000022201101221000201202020022212011 \\ 12020122202222022201111010222210120002121202 \\ 21212101100102000212021000120000021102001220 \\ 2212211020020021010000221210122221010010210 \\ 01000120111101002001201220221212212012201011 \\ 2110112010101202210202220102221012120001222 \\ 21111212200100202111210110022010000100020011 \\ 02202021101212220211100001221000111120221200 \\ 11021120212110010121020222112211012120001222 \\ 0022221001221021010202021110220022212002220 \\ 2211021111202021021110202001222200210000202 \\ 2111122112221121100221201200021112020020120 \\ 02122012122001011220120101112002122201121111 \\ 02211220122010012110011121200021201121202221 \\ 00011221222002011201002102120211101212001111 \\ 22122101200112220201122210101102110211210220 \\ 21001100002121120100112110210222010000001010 \\ 212112212200122220010112022211220212111020112 \\ 1110012011111102111010020100102221121110112 \\ 0221102111111221122210000021110201110020120 \\ 1221022222001121102201120202220101201120220 \\ 02210111211021022110000100221102122200201111 \\ 00002111112011010111211021021010110222111111 \\ 0221112022122002220100022210221122112022220 \\ 00022101212022012021111201200122200111222112 \\ 0120022122211010100202021212210000000210121 \\ 022000112120000102002022020110011022012021101 \\ 01111211002001011112021120011212122200111112 \end{array} \right)$$

$$a_{44,3} = \left(\begin{array}{c} 01222122212002101002110102200122221010010210 \\ 020110011012110111102200222002212010222112 \\ 11202001121210011100200220101112000121101202 \\ 02221100102220210220022222212202002002112 \\ 2200210202120202000111020111000212202222021 \\ 10122011202122021012212101102211001020102222 \\ 0111202221222121111210011101211020102120210 \\ 00211022100201102011111002212010201201100000 \\ 02221010012200020011120120011102221002011222 \\ 02021011102100021211221102101120221012212201 \\ 22202112111020000021111120221212101212200020 \\ 10212020220020102202201221100222201110102000 \\ 0102102212011210112110010221201211000222220 \\ 12210120111021001200012002100021020020121111 \\ 11021122120100200202211110001002210112010212 \\ 20201000121202002002211012022211001021121121 \\ 22211120000222011012210002011010100111221022 \\ 22020122202222022201111010221120210001212101 \\ 1121210110010200021202100012000012201002110 \\ 1212211102002002101000022121021112020020120 \\ 01000120111101002001201220222121121021102022 \\ 11101120101012022102022201021122021210002111 \\ 11111212200100202111210110021020000200010022 \\ 02202021101212220211100001222000222210112100 \\ 21021120212110010121020222111122021210002111 \\ 00222210012210210202021110110011121001110 \\ 12110211112020210211102020011111100120000101 \\ 11111221122211211002212012000122221010010210 \\ 01211021211002022110210202222002122201121111 \\ 01122110211020021220022212100021201121202221 \\ 0002211211100102210200120121021101212001111 \\ 21211202100221110102211120201102110211210220 \\ 2200220000121221020221220120222010000001010 \\ 22122112110021111002022101121220212111020112 \\ 1220021022222201222020010200102221121110112 \\ 0112201222222112221120000011110201110020120 \\ 11120111111002212201102210102220101201120220 \\ 01120222122012011220000200111102122200201111 \\ 0000122221022020222122012011010110222111111 \\ 0112221011211001110200011120221122112022220 \\ 00011202121011021012222102100122200111222112 \\ 02100111211122020200101012122210000000210121 \\ 01100022121000020100101102200111022012021101 \\ 02222122001002022221012210021212122200111112 \end{array} \right)$$

$$a_{44,4} = \left(\begin{array}{c} 01222122212002101002110102200211112020020120 \\ 0201100110121101111022002220011121020111220 \\ 11202001121210011100200220102221000212202101 \\ 022211001022202102200222221121101001001222 \\ 22002102021202020001110201110000121101111010 \\ 10122011202122021012212101101122002010201111 \\ 01112022212221211112100111011220102012101022 \\ 0021102210020110201111002211020102102200001 \\ 02221010012200020011120120012201112001022110 \\ 02021011102100021211221102102210112021121100 \\ 22202112111020000021111120222121202121100012 \\ 10212020220020102202201221100111102220201000 \\ 01021022120112101121100102211021220001111112 \\ 12210120111021001200012002100012010010212222 \\ 11021122120100200202211110002001120221020120 \\ 20201000121202002002211012021122002012212211 \\ 22211120000222011012210002012020200222112011 \\ 22020122202222022201111010222210120002121202 \\ 11212101100102000212021000120000021102001222 \\ 12122111020020021010000221210122221010010210 \\ 01000120111101002001201220221212212012201010 \\ 1110112010101202210202220102221012120001220 \\ 11111212200100202111210110022010000100020011 \\ 02202021101212220211100001221000111120221202 \\ 21021120212110010121020222112211012120001220 \\ 002222100122102102020211110220022212002221 \\ 1211021111202021021110202001222200210000202 \\ 11111221122211211002212012000211112020020120 \\ 0020022012100202200211122112021121101202221 \\ 00022101121011020222002211211200020021010002 \\ 01122102221000022010020222101120220112112222 \\ 10200012202110201010110000112011202111021002 \\ 11001100002121120100112110210222010000001010 \\ 12022102222010200110002022222102001011101221 \\ 2221100110112110220001110111011010021221221 \\ 00022202110110222201201120002022020010101202 \\ 20021100221002102211222210210102220101201002 \\ 00021022210022000222021220202011211100012221 \\ 011100221110120212202021110022220212222222 \\ 0221112022122002220100022210221122112022221 \\ 01100012211020020100102021211001022011000222 \\ 02011100121212021212220111220122122200021202 \\ 000112222110010210122200211110201111212102211 \\ 0222212200100202222101221002212121100222221 \end{array} \right)$$

$$a_{44,5} = \left(\begin{array}{c} 01222122212002101002110102200122221010010210 \\ 020110011012110111102200222002212010222110 \\ 11202001121210011100200220101112000121101202 \\ 02221100102220210220022222212202002002111 \\ 2200210202120202000111020111000212202222020 \\ 10122011202122021012212101102211001020102222 \\ 01112022212221211112100111012110201021202111 \\ 00211022100201102011111002212010201201100002 \\ 02221010012200020011120120011102221002011220 \\ 02021011102100021211221102101120221012212200 \\ 22202112111020000021111120221212101212200021 \\ 10212020220020102202201221100222201110102000 \\ 0102102212011210112110010221201211000222221 \\ 12210120111021001200012002100021020020121111 \\ 11021122120100200202211110001002210112010210 \\ 20201000121202002002211012022211001021121122 \\ 22211120000222011012210002011010100111221022 \\ 22020122202222022201111010221120210001212101 \\ 1121210110010200021202100012000012201002111 \\ 1212211102002002101000022121021112020020120 \\ 01000120111101002001201220222121121021102020 \\ 11101120101012022102022201021122021210002110 \\ 11111212200100202111210110021020000200010022 \\ 02202021101212220211100001222000222210112101 \\ 21021120212110010121020222111122021210002110 \\ 00222210012210210202021110110011121001112 \\ 12110211112020210211102020011111100120000101 \\ 11111221122211211002212012000122221010010210 \\ 0010011021200101100122211221021121101202221 \\ 00011202212022010111001122121200020021010002 \\ 02211201112000011020010111201120220112112222 \\ 20100021101220102020220000222011202111021002 \\ 2200220000121221020221220120222010000001010 \\ 21011201111020100220001011112102001011101221 \\ 11122002220221220110002220221011010021221221 \\ 00011101220220111102102210002022020010101202 \\ 10012200112001201122111120120102220101201002 \\ 00012011120011000111012110102011211100012221 \\ 0222001122202101211010122200222202122222222 \\ 01122210112110011102000111202211221112022221 \\ 02200021122010010200201012121001022011000222 \\ 01022200212121012121110222110122122200021202 \\ 0002211122002012021110012221020111212102211 \\ 0111121100200101111202112001212121100222221 \end{array} \right)$$

$$a_{44,6} = \left(\begin{array}{c} 01222122212002101002110102200211112020020120 \\ 0201100110121101111022002220011121020111221 \\ 11202001121210011100200220102221000212202101 \\ 0222111001022202102200222221121101001001221 \\ 22002102021202020001110201110000121101111012 \\ 10122011202122021012212101101122002010201111 \\ 01112022212221211112100111011220102012101020 \\ 0021102210020110201111002211020102102200000 \\ 02221010012200020011120120012201112001022111 \\ 02021011102100021211221102102210112021121102 \\ 2220211211102000002111120222121202121100010 \\ 10212020220020102202201221100111102220201000 \\ 0102102212011210112110010221102122000111110 \\ 12210120111021001200012002100012010010212222 \\ 11021122120100200202211110002001120221020121 \\ 20201000121202002002211012021122002012212212 \\ 2221112000022201101221000201202020022212011 \\ 22020122202222022201111010222210120002121202 \\ 11212101100102000212021000120000021102001220 \\ 12122111020020021010000221210122221010010210 \\ 01000120111101002001201220221212212012201011 \\ 11101120101012022102022201022211012120001222 \\ 11111212200100202111210110022010000100020011 \\ 02202021101212220211100001221000111120221200 \\ 21021120212110010121020222112211012120001222 \\ 00222210012210210202021110220022212002220 \\ 1211021111202021021110202001222200210000202 \\ 1111122112221121100221201200021112020020120 \\ 02122012122001011220120101112002122201121111 \\ 02211220122010012110011121200021201121202221 \\ 00011221222002011201002102120211101212001111 \\ 12122101200112220201122210101102110211210220 \\ 11001100002121120100112110210222010000001010 \\ 11211221220012222001011202211220212111020112 \\ 2110012011111102111010020100102221121110112 \\ 0221102111111221122210000021110201110020120 \\ 22210222222001121102201120202220101201120220 \\ 02210111211021022110000100221102122200201111 \\ 00002111112011010111211021021010110222111111 \\ 02211120221220022201000222102211221112022220 \\ 00022101212022012021111201200122200111222112 \\ 0120022122211010100202021212210000000210121 \\ 022000112120000102002022020110011022012021101 \\ 01111211002001011112021120011212122200111112 \end{array} \right)$$

$$a_{44,7} = \left(\begin{array}{c} 02111211121001202001220201100211112020020120 \\ 020110011012110111102200222002212010222112 \\ 2120200112121001100200220101112000121101202 \\ 022211001022202102200222222212202002002112 \\ 1200210202120202000111020111000212202222021 \\ 20122011202122021012212101102211001020102222 \\ 0111202221222121111210011101211020102120210 \\ 0021102210020110201111002212010201201100000 \\ 02221010012200020011120120011102221002011222 \\ 02021011102100021211221102101120221012212201 \\ 1220211211102000002111120221212101212200020 \\ 20212020220020102202201221100222201110102000 \\ 0102102212011210112110010221201211000222220 \\ 22210120111021001200012002100021020020121111 \\ 21021122120100200202211110001002210112010212 \\ 10201000121202002002211012022211001021121121 \\ 12211120000222011012210002011010100111221022 \\ 12020122202222022201111010221120210001212101 \\ 2121210110010200021202100012000012201002110 \\ 221221102002002101000022121021112020020120 \\ 01000120111101002001201220222121121021102022 \\ 21101120101012022102022201021122021210002111 \\ 21111212200100202111210110021020000200010022 \\ 02202021101212220211100001222000222210112100 \\ 11021120212110010121020222111122021210002111 \\ 002222100122102102020211110110011121001110 \\ 22110211112020210211102020011111100120000101 \\ 21111221122211211002212012000122221010010210 \\ 01211021211002022110210202222002122201121111 \\ 01122110211020021220022212100021201121202221 \\ 0002211211100102210200120121021101212001111 \\ 11211202100221110102211120201102110211210220 \\ 1200220000121221020221220120222010000001010 \\ 12122112110021111002022101121220212111020112 \\ 2220021022222201222020010200102221121110112 \\ 0112201222222112221120000011110201110020120 \\ 21120111111002212201102210102220101201120220 \\ 01120222122012011220000200111102122200201111 \\ 0000122221022020222122012011010110222111111 \\ 0112221011211001110200011120221122112022220 \\ 00011202121011021012222102100122200111222112 \\ 02100111211122020200101012122210000000210121 \\ 01100022121000020100101102200111022012021101 \\ 02222122001002022221012210021212122200111112 \end{array} \right)$$

$$a_{44,8} = \left(\begin{array}{c} 02111211121001202001220201100122221010010210 \\ 0201100110121101111022002220011121020111220 \\ 2120200112121001100200220102221000212202101 \\ 022211001022202102200222221121101001001222 \\ 12002102021202020001110201110000121101111010 \\ 20122011202122021012212101101122002010201111 \\ 01112022212221211112100111011220102012101022 \\ 0021102210020110201111002211020102102200001 \\ 02221010012200020011120120012201112001022110 \\ 02021011102100021211221102102210112021121100 \\ 12202112111020000021111120222121202121100012 \\ 20212020220020102202201221100111102220201000 \\ 01021022120112101121100102211021220001111112 \\ 22210120111021001200012002100012010010212222 \\ 21021122120100200202211110002001120221020120 \\ 10201000121202002002211012021122002012212211 \\ 1221112000022201101221000201202020022212011 \\ 12020122202222022201111010222210120002121202 \\ 21212101100102000212021000120000021102001222 \\ 2212211020020021010000221210122221010010210 \\ 01000120111101002001201220221212212012201010 \\ 2110112010101202210202220102221012120001220 \\ 21111212200100202111210110022010000100020011 \\ 02202021101212220211100001221000111120221202 \\ 11021120212110010121020222112211012120001220 \\ 00222210012210210102020211110220022212002221 \\ 2211021111202021021110202001222200210000202 \\ 21111221122211211002212012000211112020020120 \\ 0020022012100202200211122112021121101202221 \\ 00022101121011020222002211211200020021010002 \\ 01122102221000022010020222101120220112112222 \\ 20200012202110201010110000112011202111021002 \\ 21001100002121120100112110210222010000001010 \\ 22022102222010200110002022222102001011101221 \\ 12211001110112110220001110111011010021221221 \\ 00022202110110222201201120002022020010101202 \\ 10021100221002102211222210210102220101201002 \\ 00021022210022000222021220202011211100012221 \\ 011100221110120212202021110022220212222222 \\ 0221112022122002220100022210221122112022221 \\ 01100012211020020100102021211001022011000222 \\ 02011100121212021212220111220122122200021202 \\ 000112222110010210122200211110201111212102211 \\ 0222212200100202222101221002212121100222221 \end{array} \right)$$

Appendix F

The matrix a

We display the matrix a as a MAGMA input. This matrix has been obtained by applying the algorithm of Chapter 4 to the matrix $a_{44,1}$ of Appendix E.

